

€

GCSE Mathematics Higher Tier Number Algebra Ratio, proportion and rates of change Geometry & measures Probability Statistics

Here is pretty much all the Higher Tier content we could fit onto an A3 sheet of paper, including all the formulae you are required to know for GCSE. An \rightarrow points to an illustrative example. The codes refer to the DfE subject content. Pin this to a wall, keep it on your desk, carry it in your bag, make notes on it (sorry, don't take it into the examination).

Iteration

 θ°

0

30

45

60

90

 $\sin \theta^{\circ}$

0

1

√3

2

1

segment

theorem

cross

Enlargement

• Clockwise or anticlockwise the shape will get smaller).

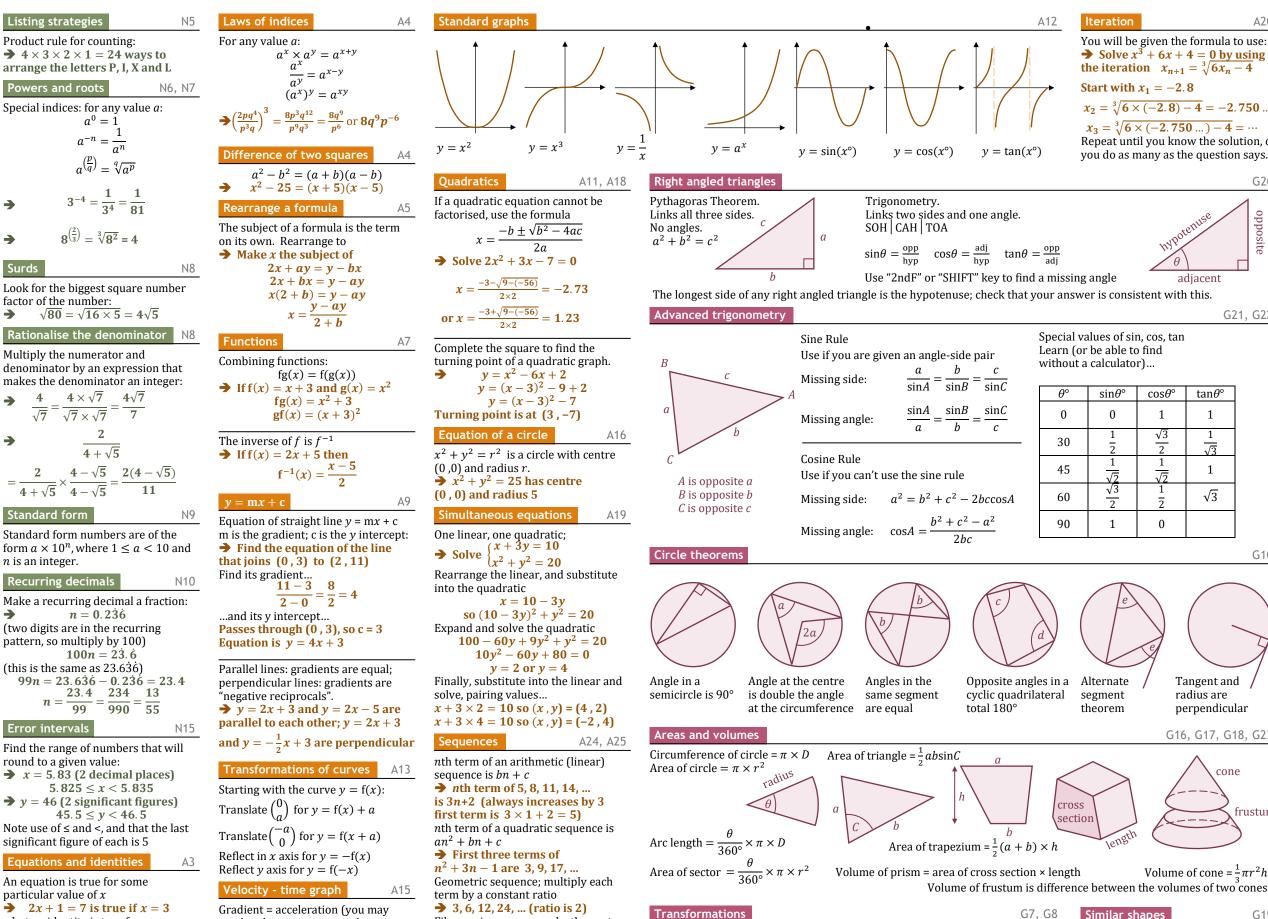
Centre of enlargement

• Scale factor (if -1 < SF < 1

section

• Area

Volume



Fibonacci sequence; make the next

term by adding the previous two ...

➔ 2, 4, 6, 10, 16, 26, 42, ...

Reflection

Translation

• Vector

• Line of reflection

Rotation

Centre of rotation

Angle of rotation

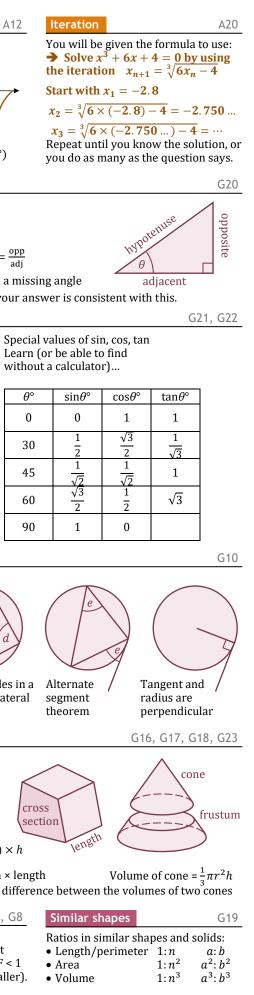
...but an identity is true for every value of x

need to draw a tangent to the curve at

Area under curve = distance travelled.

a point to find the gradient);

 $(x+a)^2 \equiv x^2 + 2ax + a^2$ (note the use of the symbol \equiv)



Percentages: multipliers R9, R16
Percentage increase or decrease; use a multiplier (powers for repetition) → Initially there were 20 000 fish in a lake. The number decreases by 15% each year. Estimate the number of fish after 6 years. 20 000 × 0.85 ⁶ = 7500 (2sf)
Formula for compound interest $r > n$
Total accrued = $P\left(1 + \frac{r}{100}\right)^n$ → I invest £600 at 3% compound interest. What is my account worth after 5 years? £600 × $\left(1 + \frac{3}{100}\right)^5$ = £695.56
Direct & inverse proportion R10
<i>y</i> is directly proportional to <i>x</i> :
y = kx for a constant k b is directly proportional to a^2 a = 6 when b = 90 Find b if a = 8 b = ka ² a = 6 and b = 90 for k 90 = k × 6 ² so k = 2.5, b = 2.5a ² b = 2.5 × 8 ² = 160 y is inversely proportional to x yx = k or y = $\frac{k}{x}$ for a constant k
<i>x</i>
Probability rules P8, P9
Multiply for independent events P(6 on dice and H on coin) $\frac{1}{6} \times \frac{1}{2} = \frac{1}{12}$ Add for mutually exclusive events P(5 or 6 on dice) $\frac{1}{6} + \frac{1}{6} = \frac{2}{6}$ Apply these rules to tree diagrams.
In general P(A or B) = P(A) + P(B) - P(A and B) $P(A \text{ and } B) = P(A \text{ given } B) \times P(B)$
Histograms S3
Frequency = frequency density multiplied by class width. This means that bars with the same frequency have the same area.
titequency density edual areas; edual teduencies
Box plots S4
Interquartile range (IQR) = UQ – LQ

minimum lower quartile (LQ)

median

upper quartile (UQ)

maximum