$\xrightarrow{\rightarrow} 4 \times 3 \times 2 \times 1=24$ ways to arrange the letters P, I, X and L

| Powers and roots $\quad N 6$, |  |
| ---: | :--- |
| Special indices: for any value $a$ : |  |
| $a^{0}$ | $=1$ |
| $a^{-n}$ | $=1$ |

$a^{-n}=\frac{1}{a^{n}}$
$a^{\left(\frac{p}{q}\right)}=\sqrt[a]{a^{p}}$
$\Rightarrow \quad 3^{-4}=\frac{1}{3^{4}}=\frac{1}{81}$
$\Rightarrow \quad 8^{\left(\frac{2}{3}\right)}=\sqrt[3]{8^{2}}=4$
Surds

## Laws of indice

## N6, N7

$$
\Rightarrow\left(\frac{2 p q^{4}}{p^{3} q}\right)^{3}=\frac{8 p^{3} q^{12}}{p^{4} q^{3}}=\frac{8 q^{9}}{p^{6}} \text { or } 8 q^{9} p^{-6}
$$

Difference of two squares A4

$$
\begin{aligned}
& a^{2}-b^{2}=(a+b)(a-b) \\
& x^{2}-25=(x+5)(x-5)
\end{aligned}
$$

$\qquad$
Rearrange a formula A5
The subject of a formula is the ter $\rightarrow$ Make $x$ the subject of
$2 x+a y=y-b x$
$2 x+b x=y-a y$
$x(2+b)=y-a y$
$x=\frac{y-a y}{2+b}$

## Functions



Combining functions:

$\mathrm{fg}(x)=x^{2}+3$
$\mathrm{gf}(x)=(x+3)^{2}$
The inverse of $f$ is $f^{-1}$
$\rightarrow$ If $\mathrm{f}(x)=2 x+5$ then
$y=\mathrm{m} x+\mathrm{c}$
$(x)=\frac{x}{2}$
$y=\mathrm{m} x+\mathrm{c} \quad$ A9
Equation of straight line $y=m x+c$
m is the gradient; c is the $y$ intercept:
$\Rightarrow$ is the gradient; $c$ is the $y$ intercept: that joins $(0,3)$ to $(2,11)$ Find its gradient....

- $\frac{-0}{2-0}=\frac{8}{2}=4$
...and its y intercept... . Passes through $(0,3)$ so $\mathrm{c}=3$
Equation is $y=4 x+3$
Parallel lines: gradients are equal; perpendicular lines: gradients are "negative reciprocals".
$\Rightarrow y=2 x+3$ and $y=2 x-5$ are parallel to each other; $y=2 x+3$ and $y=-\frac{1}{2} x+3$ are perpendicular Transformations of curves A13 Starting with the curve $y=\mathrm{f}(x)$ : Translate $\binom{0}{a}$ for $y=\mathrm{f}(x)+a$
Translate $\binom{-a}{0}$ for $y=\mathrm{f}(x+a)$
Reflect in $x$ axis for $y=-\mathrm{f}(x)$
Reflect $y$ axis $\mathrm{for} y=\mathrm{f}(-x)$
Reffect in $y$ axis for $y=\mathrm{f}(-x)$
Velocity - time graph
An_A15
Gradient = acceleration (you may need to draw a tangent one the find the gradient): Area under curve = distance travelled.

A4

Quadratics A11, A18 If a quadratic equation cannot be factorised, use the formula

$$
x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}
$$

$\Rightarrow$ Solve $2 x^{2}+\begin{gathered}2 a \\ x-7\end{gathered}=0$
$x=\frac{-3-\sqrt{9-(-56)}}{2 \times 2}=-2.73$
or $x=\frac{-3+\sqrt{9-(-56)}}{2 \times 2}=1.23$
Complete the square to find the turning point of a quadratic graph.
$\Rightarrow \quad \begin{aligned} & y=x^{2}-6 x+2 \\ & y=(x-3)^{2}-9+2\end{aligned}$

$$
\begin{gathered}
y=(x-3)^{2}-9+2 \\
y=(x-3)^{2}-7 \\
\text { ng point is at }(3,-7)
\end{gathered}
$$

Turning point is at $(3,-7)$
Equation of a circle
$x^{2}+y^{2}=r^{2}$ is a circle with centre
$x^{2}+y^{2}=r^{2}$ is a circle with ce
$(0,0)$ and radius $r$.
$\xrightarrow{(0,0) \text { and radius } r \text {. }} x^{2}+y^{2}=25$ has centre
$(0,0)$ and radius 5
Simultaneous equations A19
One linear, one quadratic;
$\rightarrow$ Solve $\left\{\begin{array}{l}x+3 y=10 \\ x^{2}+y^{2}=20\end{array}\right.$
Rearrange the linear, and substitute into the quadratic
$x=10-3 y$
so $(10-3 y)^{2}+y^{2}=20$
Expand and solve the quadratic Expand and solve the quadratic
$100-60 y+9 y^{2}+y^{2}=20$ $10 y^{2}-60 y+80=0$
Finally, substitute into the linear and
solve, pairing values...
solve, pairing values...
$x+3 \times 2=10$ so $(x, y)=(4,2)$
$x+3 \times 4=10$ so $(x, y)=(-2,4)$
Sequences
A24, A25
$n$th term of an arithmetic (linear)
sequence is $b n+c$
$\rightarrow n$th term of $5,8,11,14, \ldots$ is $3 n+2$ (always increases by 3 first term is $3 \times 1+2=5$ ) $n$th term of a quadratic sequence is $\Rightarrow n^{2}+b n+c$
$\overrightarrow{n^{2}}+3 n-1$ are $3,9,17$,
Geometric sequence; multiply each term by a constant ratio
$\overrightarrow{7} 3,6,12,24, \ldots$ (ratio is 2 ) Fibonacci sequence; make the next $\xrightarrow{\text { term by adding the previous }}$



Trigonometry
Links two sides and one angle.
SOH $\mathrm{CAH} \mid$ TOA SOH | САН | TOA
$\sin \theta=\frac{\mathrm{opp}}{\text { hyp }} \quad \cos \theta=\frac{\mathrm{adj}}{\mathrm{hyp}} \quad \tan \theta=\frac{\mathrm{opp}}{\mathrm{adj}}$
Use "2ndF" or "SHIFT" key to find a missing angle
12 Iteration
You will be given the formula to use $\Rightarrow$ Solve $x^{3}+6 x+4=0$ by using the iteration $=\sqrt[3]{6 x_{n}-4}$ Start with $x_{1}=-2.8$
$x_{2}=\sqrt[3]{6 \times(-2.8)-4}=-2.750$ $x_{3}=\sqrt[3]{6 \times(-2.750 \ldots)-4}=$ Repeat until you know the solution, or
you do as many as the question says.

The longest side of any right angled triangle is the hypotenuse; check that your answer is consistent with this.

## Advanced trigonometry

| Sine Rule |  |
| :---: | :---: |
| Use if you are given an angle-side pair |  |
| Missing side: | $\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$ |
| Missing angle: | $\frac{\sin A}{a}=\frac{\sin B}{b}=\frac{\sin C}{c}$ |
| Cosine Rule |  |
| Use if you can't use the sine rule |  |
| Missing side: | $a^{2}=b^{2}+c^{2}-2 b c \cos A$ |
| Missing angle: | $\cos A=\frac{b^{2}+c^{2}-a^{2}}{2 b}$ |

Special values of $\sin , \cos , \tan$
Learn (or be able to find
without a calculator)...

| $\theta^{\circ}$ | $\sin \theta^{\circ}$ | $\cos \theta^{\circ}$ | $\tan \theta^{\circ}$ |
| :---: | :---: | :---: | :---: |
| 0 | 0 | 1 | 1 |
| 30 | $\frac{1}{2}$ | $\frac{\sqrt{3}}{2}$ | $\frac{1}{\sqrt{3}}$ |
| 45 | $\frac{1}{\sqrt{2}}$ | $\frac{1}{\sqrt{2}}$ | 1 |
| 60 | $\frac{\sqrt{3}}{2}$ | $\frac{1}{2}$ | $\sqrt{3}$ |
| 90 | 1 | 0 |  |

## Circle theorems



## Circumference of circle $=\pi \times D \quad$ Area of triangle $=\frac{1}{2} a b \sin C$

Area of circle $=\pi \times r$

Arc length $=\frac{\theta}{360^{\circ}} \times \pi \times D$


Area of trapezium $=\frac{1}{2}(a+b) \times h$


Area of sector $=\frac{\theta}{360^{\circ}} \times \pi \times r^{2}$
Volume of prism $=$ area of cross section $\times$ length


Percentages: multipliers R9, R16
Percentage increase or decrease; use multiplier (powers for repetition) $\rightarrow$ Initially there were 20000 fish a lake. The number decreases by $15 \%$ each year. Estimate the $20000 \times 0.85^{6}=7500(2 \mathrm{sf})$

Formula for compound interest
Total accrued $=P\left(1+\frac{r}{100}\right)^{n}$
$\rightarrow$ I invest $£ 600$ at $3 \%$ compound interest. What is my account worth $£ 600 \times\left(1+\frac{3}{100}\right)^{5}=£ 695.56$

## Direct \& inverse proportion R10

is directly proportional to $x$ :
$y=k x$ for a constant $k$
$b$ is directly proportional to $a^{2}$ $\overrightarrow{ } \vec{b}$ is directly proportional to $a^{2}$
$a=6$ when $b=90$ Find $b$ if $a=8$ $=6$ when $b=90 \quad$ Find $b$ if $a=8$ $b=k a^{2} \quad a=6$ and $b=90$ for $k$
$90=k \times 6^{2}$ so $k=2.5, b=2.5 a^{2}$ $90=k \times 6^{2}$ so $k=2.5, b=2.5 \times 160$
$b$ is inversely proportional to $x$ $y$ is inversely proportional to $x$ $y x=k$ or $y=\frac{k}{x}$ for a constant $k$

## Probability rules

$\rightarrow \mathrm{P}(6$ on dice and H on conts $)$

$$
\frac{1}{6} \times \frac{1}{2}=\frac{1}{12}
$$

Add for mutually exclusive events
$\rightarrow \mathrm{P}(5$ or 6 on dice $)$
Apply these rules to tree diagrams.
In general... $\mathrm{P}(A$ and $B)=\mathrm{P}(A$ given $B) \times \mathrm{P}(B)$
Histograms
Frequency = frequency density
multiplied by class width. This ultiplied by class width. This mea have the same area.


Box plots S4
Interquartile range (IQR) = UQ - LQ

| , |  |
| :---: | :---: |
|  |  |

